

# Activities of IMI-BAS in data protection

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Department of Mathematical Foundations of Informatics - since  
1988, founded by Stefan Dodunekov (1945-2012)  
Coding Theory – Cryptology  
Theory and Applications

- The cryptology studies the mathematical techniques to ensure data security and methods for attack and defence.
- Mathematics in Cryptology:
  - Discrete Mathematics
  - Number theory, Algebra
  - Geometry
  - Coding theory – over 300 papers since 1975 in specialized international journals



# Challenges to the Cryptography

- Post quantum Cryptography
- Longlasting security: 50 - 100 years
- Security for cloud technologies
- Authentication Cryptology
- Low-energy applications (lightweight cryptography)



# McEliece public key system

- Proposed in 1978 by Robert McEliece
- Strong candidate for post-quantum algorithm
- Based on the difficulties in solving decoding problems
  - The private key uses a linear code with known effective decoding
  - The public key proposes difficult decoding problem
- No known successful attacks
- In particular – resistant to Shor attack

# Mathematics behind the McEliece system

Let  $\mathbf{C}$  be a binary  $[n, k]$  code which is able to correct  $t$  errors,  $\mathbf{S}$  be a binary non-singular  $k \times k$  matrix,  $\mathbf{P}$  be a permutation  $n \times n$  matrix. Calculate the matrix

$$\mathbf{G}^* = \mathbf{SGP},$$

where  $\mathbf{G}$  is a  $k \times n$  generator matrix of  $\mathbf{C}$ .

Encryption:

- (1) Divide the message into blocks of length  $k$ ; let  $\mathbf{v}$  be such a block;
- (2) Calculate  $\mathbf{vG}^*$ ;
- (3) Invert randomly  $t$  bits in  $\mathbf{vG}^*$ ;
- (4) The cryptotext is

$$\mathbf{w} = \mathbf{vG}^* + \mathbf{e},$$

where  $\mathbf{e}$  is random vector (corresponding to the changes in (3)) of weight  $t$ .

The matrix  $\mathbf{G}^*$  (the encryption key) is public, the matrices  $\mathbf{S}$ ,  $\mathbf{G}$  and  $\mathbf{P}$  are kept secret.

# Advanced Encryption Standard (AES)

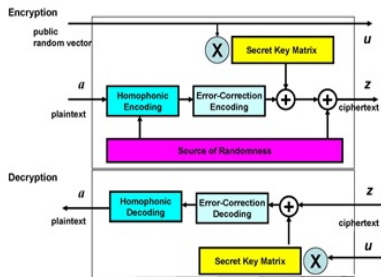
- Accepted by National Institute of Standards and Technology (NIST) of USA in 2001
- According to the validation list of NIST (<http://csrc.nist.gov/groups/STM/cavp/documents/aes/aesval.html>) there are (at least) 2662 implementations
- 2003: AES-128 for **classified information**, AES-192/-256 for **top secret information**
- Many attack; no known successful attack
- The diffusion in the algorithm is ensured by MDS codes
- Bulgarian contributions to the theory of MDS codes – Dodunekov, Landjev (over 10 papers)

- Low:
  - energy consumption
  - implementation resources
  - computational efforts
- Authentication by Niederreiter cryptosystem
  - Modification from a McEliece system; developed in 1986 by Harald Niederreiter
  - Uses the syndrome as cryptotext; the message is the error vector



# Homophonic coding and error-correcting coding

- The homophonic coding ensures randomization of the plaintext
- Against statistical attacks



- **Enhancing Cryptographic Primitives with Techniques from Error Correcting Codes** Veliko Tarnovo, October 6-9, 2008



- Design and Security of Cryptographic Functions, Algorithms and Devices  
([https://www.cosic.esat.kuleuven.be/summer\\_school\\_albena/](https://www.cosic.esat.kuleuven.be/summer_school_albena/))  
Albena, June 30 - July 5, 2013
  - 24 lecturers from Austria, Belgium, Germany, Denmark, Israel, Ireland, Norway, USA, France, The Netherlands, Switzerland
  - Bart Preneel - chair of International Association for Cryptologic Research
  - Vincent Rijmenen - one of the proposers of AES

- **BalkanCrypt Kickoff Meeting and Workshop**  
(<http://balkancrypt.uist.edu.mk/>) Sofia, November 7-8, 2013
  - 40 participants from Balkan countries, Belgium, Germany, Norway, Japan
  - Bart Preneel
  - Hideki Imai - chair of CRYPTREC (Cryptography Techniques Research and Evaluation Committee of Japan)
  
- Bulgaria will organize **EUROCRYPT 2015**